# On the fly handling of missing data in the application of prediction models: a comparison of methods

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# Abstract

**Introduction –** The occurrence of real-time missing predictor values is unique to the application of prediction models and seems to be underrepresented in the literature. In this study, we aim to evaluate various real-time strategies to handle the pervasive problem of missing data when using clinical data. We aim to evaluate the influence of built-in missing data handling mechanisms on prediction accuracy and compare it with existing real-time imputation methods (e.g., joint modelling imputation). We evaluate the effect of various missing data handling methods under specific missing data circumstances as would occur in medical practice.

**Methods –**

**Results –**

**Discussion –**

# Introduction

Incompleteness of medical records is a ubiquitous problem when using healthcare data. Besides the well documented issues that missing data can create in data analyses, incompleteness of medical records may also create practical issues in clinical practice (1,2). For instance, a prediction model that relies on historical but unrecorded data for a particular patient or prediction models that are used as early-warning systems for individual patients (3,4). Most prediction models are not designed to be used when predictors are not fully observed, and ad-hoc approaches such as replacing the missing value with the population average value (i.e., mean imputation) is generally not advised (1,5). As prediction models are increasingly being integrated in the electronic health record (EHR) via clinical decision support systems (CDSS), the substantial impediment of missing data on the direct use of prediction models in individual patients becomes more evident (6,7). The issue is further compounded as the (gold) standard strategies to mend or circumvent missing data are not suited for use in individual patient data in live clinical practice.

Various strategies to handle challenging manifestations of missing data have been studied thoroughly and can usually provide more plausible substitution values (e.g., via imputation) (2). Multiple imputation is often considered to be the gold standard and can provide valid estimates and correct standard errors when the missing data are missing completely at random (MCAR, when missing data is unrelated to the data) or missing at random (MAR, when missing data is dependent on observed values) (8). Most imputation algorithms, however, require direct access to data from multiple instances (i.e., multiple patients or multiple measurements) and are therefore not suitable for use on a case-by-case basis. Further, when a prediction model is applied to a single patient in clinical practice via a CDSS there is (usually) no access to any data from other individuals due to computational and privacy constraints [ref].

An intuitive alternative to imputation is to solve the missingness inside the prediction model instead of the data. Two promising methods of this type are surrogate splitting and pattern mixture modeling. The surrogate split approach is natural to random forest models (9,10). Briefly, these surrogate splits attempt to preserve the partitioning of the original split by finding the second most optimal split given other observed variables. When the model is applied, each original split for which the predictor is missing is replaced by the best available ‘surrogate’ variable, or split, to decide the split direction (9,10). The pattern sub models, which can be used for a variety of modelling techniques (e.g., regression), approach the missing data by developing, for each (possible) pattern of missing data, a separate prediction model (11). Then, when applied to a new (out-of-sample) individual the corresponding (i.e., matching the missing data pattern in the individual) prediction model is used.

In this article we compare various real-time missing data handling approaches when implementing specific modelling techniques in live clinical practice. We use the term 'real-time' to refer to methods that can be applied to data from a single individual as would occur in clinical practice, without necessitating the use of data from other individuals at the point of care. We present an extensive simulation study and a motivating example to compare the different missing data handling strategies that can be used at the implementation level. The aim is to identify strengths and weaknesses of these approaches on the ability to estimate individualized risk, as quantified by the discrimination and calibration of the predictions.

# Methods

**Brief description**

We evaluate and compare various modelling strategies for real-time handling of missing data at the implementation level via a simulation study: (i) prediction models that adopt separate imputation models (i.e., joint modelling imputation or JMI), (ii) prediction models that adopt random forests with surrogate splits and (iii) prediction models that adopt a submodel approach (10–13).

**Missing data handling methods**

Real-time imputation via Joined Modelling Imputation (JMI)

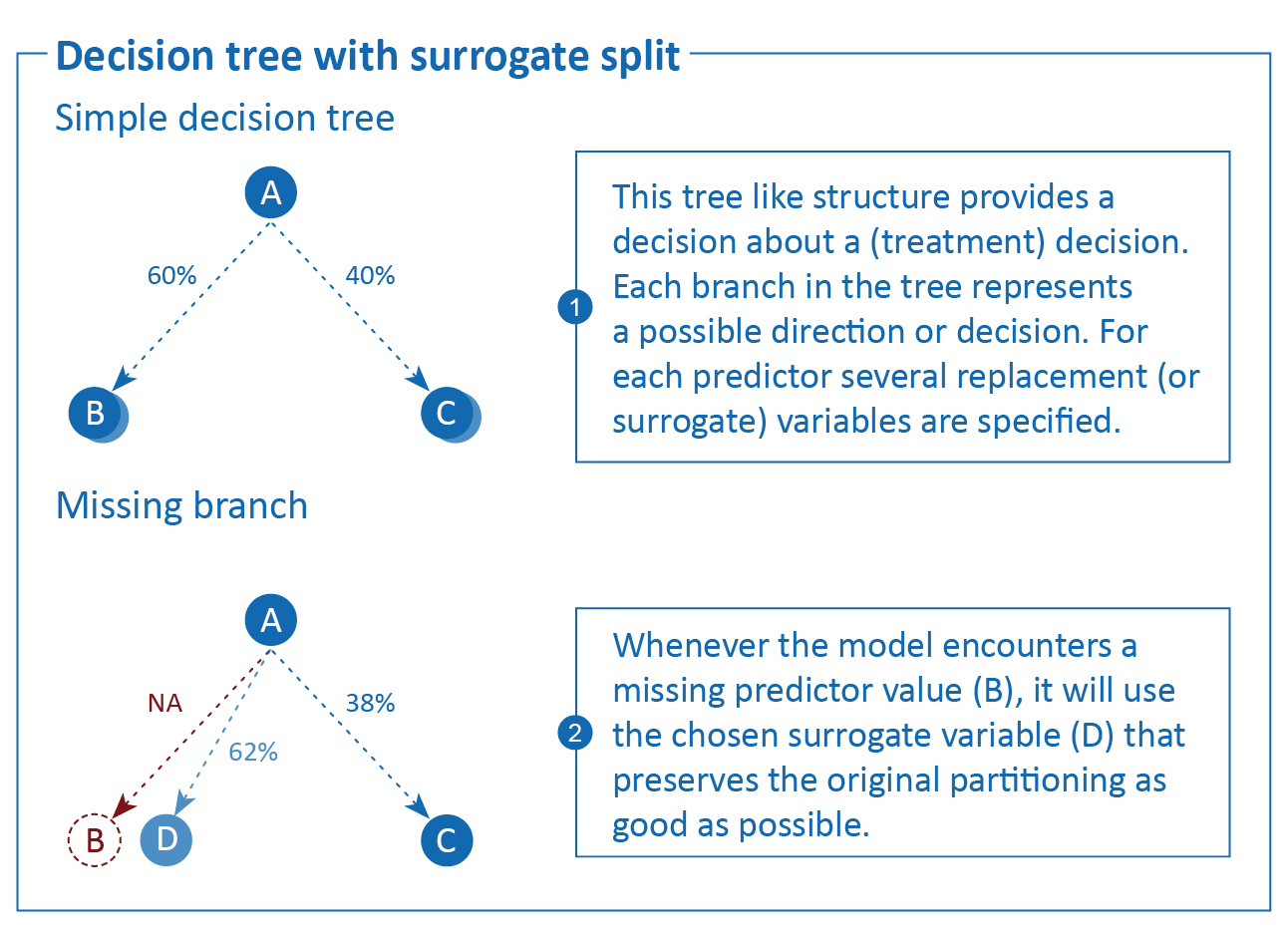
JMI is an imputation method that involves estimating the multivariate (joint) density of the data (14). JMI typically involves Monte Carlo sampling to estimate the distribution parameters and impute the missing values. Recently, an extension to JMI was proposed to allow for real-time imputation in individual patients (13,15). With the extension the development of a JMI model consists of two separate steps. In the first step, the means and covariance of all predictor variables are estimated in a development sample. Since JMI assumes that every predictor variable is normally distributed, the population characteristics (i.e., means and covariance) can directly be used to generate, or draw, imputations on an individual level. In clinical practice, when a prediction model now encounters missing values, the developed JMI model can be utilized to generate imputations for each of the missing variables. An advantage of JMI is that it can be applied to a previously developed prediction model. See Figure x for a schematic depiction of JMI.

Graphical user interface, diagram, timeline

Description automatically generated with medium confidence  
*Figure x. Joint Modelling Imputation (JMI)*

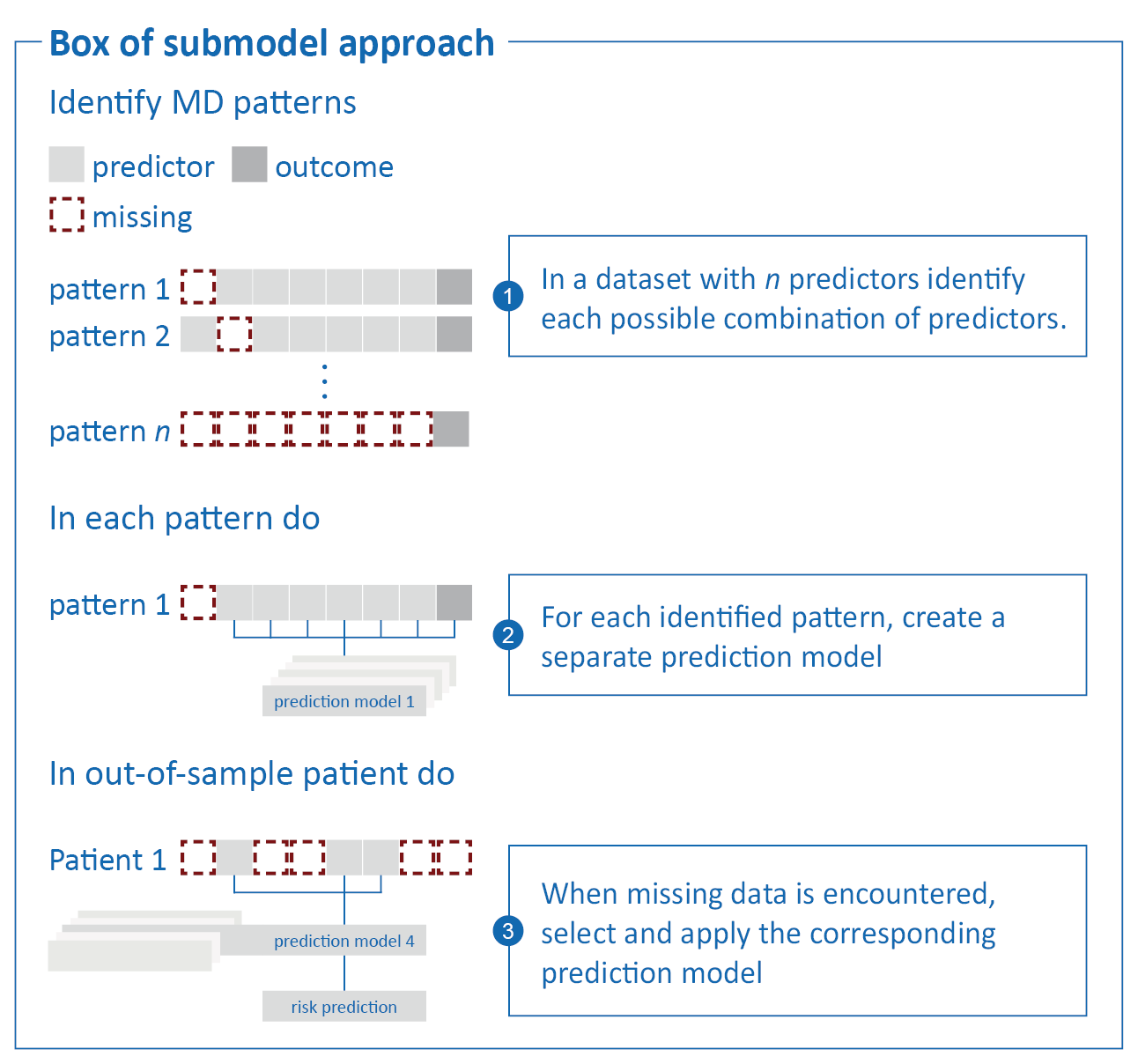
Surrogate splits

As an early extension to the well-known decision tree, surrogate splits were developed to circumvent the necessity for imputation (9,10,16). Decision trees use, as the name suggests, a tree like structure to find the optimal cut-off point which partitions the data for optimal predictive performance. Based on the values of the pre-defined predictor variables, each branch in the tree represents a possible direction or decision. In essence, random forests combine multiple decision trees to be merged for improved prediction accuracy. Briefly, surrogate splits try to preserve the partitioning of each original split in a tree as good as possible in the presence of missing predictor values. Whenever the model is applied to an individual and encounters a missing predictor value, it will use the pre-specified surrogate (i.e., replacement) variable, rather than the missing predictor variable, to decide upon the split direction. We use surrogate splits in the context of random forests. See figure x for a schematic depiction of surrogate splits.

*  
Figure x. Decision tree with surrogate splits*

Missing data pattern submodels

Another approach to address missing data without requiring imputation is to develop separate submodels for each missing data pattern (11). Each submodel is to be made specifically for one of the identified missing data patterns in the training data and the missing data patterns that are encountered in real-time clinical practice. When applied to a new, out-of-sample, individual, the collection of submodels uses the corresponding (i.e., matching the missing data pattern at hand) prediction model. A recent study has shown that the use of submodels for prediction performs similarly to multiple imputation and can be used when the data are missing not at random (MNAR, when missing data is dependent on unobserved values) (11). As such, submodels may provide an elegant and intuitive to understand method for handling missing data when implementing prediction models. See figure x for a schematic depiction of pattern submodels

  
*Figure x. Pattern submodels*

**Motivating example**

We conducted a motivational example showing the effect of the built-in methods and real-time imputation models when used in real patients. Hereto, we considered the large Medical Information Mart for Intensive Care (MIMIC)-III dataset (17). MIMIC-III provides a large database which contains information about patients staying in critical care units of the single tertiary care Beth Israel Deaconess Medical Center.

Similarly, to the simulation study, the prediction models of interest were the flexible logistic regression and random forest models. We derived both models in MIMIC-III using predictors from existing relevant prediction models using mortality as the primary outcome. For the logistic regression, we considered the Sequential Organ Failure Assessment (SOFA) prediction score and for the random forest model we considered the … (18). The SOFA score estimates the number and severity of failed organs, with in-hospital mortality as the primary outcome.

**Simulation study**

*Aims*

The aim of the simulation study is to evaluate the performance of several on-the-fly missing data handling approaches in the context of single patient application of prediction models as would occur in clinical practice (Figure x). To that end, we compare the performance of these different approaches on their calibration and discriminative performance.

**Diagram

Description automatically generated**

*Figure x. Simulation study*

*Data-generating mechanism*

All data are generated from a single model-based population, consisting of ten continuous predictors and one dichotomous outcome. In each simulation iteration, we draw two samples from the population: a complete development set (*n* = 10.000), and a validation set in which we introduce missingness to mimic how patients would present themselves in clinical practice (*n* = 20.000).

The data generating mechanism of the predictor space is a multivariate normal distribution, , with mean vector and covariance matrix Σ. All 10 predictors have a mean of zero, . The covariance matrix

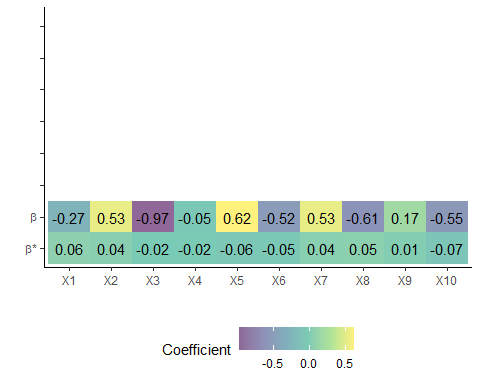
is visualized in Figure XYZ.

|  |
| --- |
| Figure XYZ. Correlation coefficients between predictors |

From the predictor space, we define the binary outcome Y. Y is a function of through the logit link function,

where s are regression coefficients, and residual error . We differentiate between three types of regression coefficients: 1) the intercept, ; 2) a vector of regression coefficients for the main effects of the predictors, ; and 3) an additional vector of regression coefficients for the interactions with the first predictor, . This introduces a polynomial effect of the second degree, , and nine moderation effects. For additional non-linearity, we use a transformation in the effect of the second predictor, . The regression coefficient vectors

are visualized in Figure XYZ. With an intercept of , the population prevalence of is 15%.

Figure XYZ. Regression coefficients of the main and interaction effects of the predictors

The validation set is amputed (i.e., made incomplete) according to several missingness mechanisms and missingness rates. In this study, we focus [exclusively?] on the Missing At Random (MAR) missingness mechanism (19). We use a mixture of the four kinds of MAR missingness, as described by [REF: Schouten]. The overall missingness rate is 60%, but within each validation set, the missingness rate varies between observations. The hypothetical patients in our validation set are missing either 40%, 60%, or 80% of the observations in the predictor space. The resulting missing data pattern is visualized in Figure x.

Chart, histogram

Description automatically generated

**Figure x.** missing data patterns.

*Missing data handling strategies*

For handling missing data in real-time, we consider JMI, surrogate splits and pattern submodels. We use JMI via three different approaches. We impute with (i) the conditional mean, (ii) a random draw from the conditional multivariate distribution and (iii) the mean of multiple (50) draws from the conditional multivariate distribution.

*Prediction models*

Each prediction model is applied to the hypothetical patients to estimate the absolute risk of the outcome for each individual observation (i.e., patient). To accommodate the use of these real-time missing data handling strategies, several types of prediction models need to be considered. We use a combination of random forests and flexible logistic regression models. We use both the random forest and logistic regression to accommodate JMI and pattern submodels. Only random forests are used to accommodate the use of surrogate splits.

*Generation of risk predictions*

The target in each risk prediction is for each prediction model to estimate the absolute risk of the outcome in each hypothetical individual observation.We evaluated the calculated risks after using five different approaches to handling missing data (Table 1). Whilst the JMI approaches and submodel approach are specifically related to the real-time imputation of missing predictor values, they are also applied to the random forest to compare between the two prediction models. The remaining strategy (i.e., surrogate splits) is specific to the prediction method used (i.e., random forest).

|  |  |  |  |
| --- | --- | --- | --- |
|  | | Flexible logistic regression | Random forest |
| JMI | Conditional mean1 | X | X |
| Random draw2 | X | X |
| Average of multiple draws3 | X | X |
| Surrogate splits4 | |  | X |
| Pattern submodels5 | | X | X |

**Table 1.** summary of missing data methods and prediction models  
  
1. Missing values are imputed by their mean conditional on the observed predictor variables; 2. Missing values are imputed by a random draw from their conditional multivariate distribution (i.e., non-deterministic imputation); 3. Missing values are imputed 50 times by a random draw from their multivariate normal distribution, The resulting 50 absolute risk predictions are then averaged to obtain the final prediction; 4. Missing values are circumvented by selecting the appropriate pattern submodel for calculating absolute risks. 5. Missing values are handled using surrogate splits.

*Performance measures*

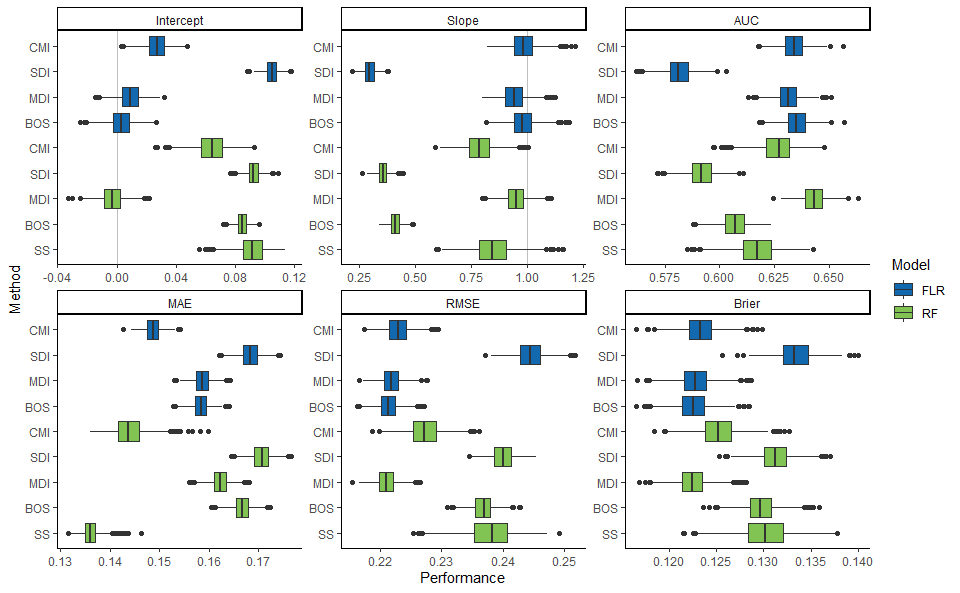
We evaluated the approaches outlined above and compared the following five performance metrics to evaluate the predicted risks under the 5 strategies: (i) root mean squared error (RMSE) of the predicted risk, (ii) brier score, (iii) concordance (C-) statistic, (iv) calibration-in-the-large (CITL) and (v) the calibration slope (Table 2).

|  |  |
| --- | --- |
| Measure | Performance metric |
| Prediction accuracy | Root mean square error (RMSE). The RMSE of the predictions reflects the error between the original predicted risk and the outcome risk which was calculated under various conditions with missing data (20). The error is presented, like the original predictions, on the probability scale. Lower values indicate better performance. |
| Brier score. The brier score calculates the squared differences between the predicted risk and the original outcome. A brier score of 0 should always reflect a perfect model, whilst the incidence of the outcome ultimately indicates what the maximum brier score is (20). |
| Discrimination | Concordance (C-)statistic. The C-statistic is a rank-order statistic, which is used to describe how well the model can discriminate between those with the event and those without. The C-statistic shows the probability of taking two random subjects (one with and one without the outcome) and correctly attributing the one with the outcome with a high risk. A C-statistic of 0.5 describes a model with no discriminative performance and a C-statistic 1 describes a model with perfect discriminative performance. |
| Calibration | Calibration-in-the-large (CITL). The CITL represents the overall calibration of a model. In other words, the extend of agreement between the average predicted risk and the original predicted risk (21). The statistic ultimately explains the amount by which the predictions systematically over or underestimate predicted risk. A value of 0 is ideal and represents perfect agreement. |
| The calibration slope. In contrast with the CITL, the calibration slope does not evaluate the average predicted, or original, risk. Rather, it quantifies the extent by which the predicted risks are too extreme (i.e., <1) or too narrow (i.e., >1) when compared with the original risk over the whole range of predicted risks. Ideally the slope is 1. |

**Table 2.** performance measures

Results [work in progress]

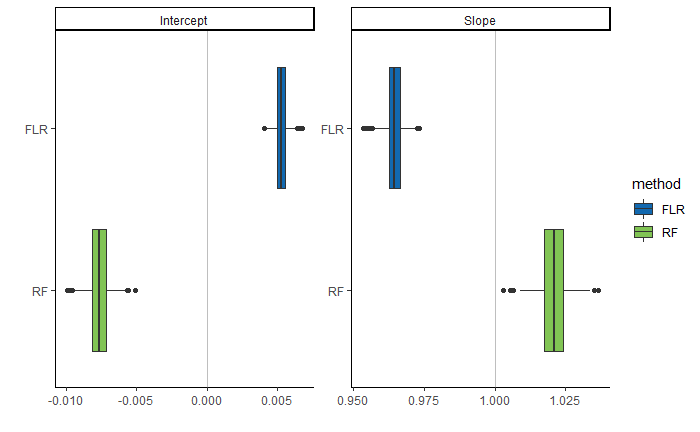
Results of the simulation study are visualized in Figure x. Table XYZ presents average performances across simulations. To give a frame of reference for interpreting performances on the incomplete validation data, we first provide the performance of the two prediction models on the complete development data. [TODO: Think about logical order of the performance measures]

 **Figure x.** Performance measures per method  
Note. CMI: conditional mean imputation; SDI: single draw imputation; MDI: multiple draw imputation; BOS: bag of submodels; SS: surrogate splits; AUC: area under the curve; MAE: mean absolute error; RMSE: root mean squared error; FLR: flexible logistic regression; RF: random forest

|  |  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- | --- |
| Label | Method | Intercept | Slope | AUC | RMSE | Brier | MAE |
| FLR | CMI | 0.027 | 0.984 | 0.634 | 0.223 | 0.123 | 0.149 |
| SDI | 0.105 | 0.297 | 0.581 | 0.244 | 0.133 | 0.168 |
| MDI | 0.009 | 0.94 | 0.631 | 0.222 | 0.123 | 0.159 |
| Submodels | 0.003 | 0.981 | 0.635 | 0.221 | 0.123 | 0.158 |
| RF | CMI | 0.064 | 0.788 | 0.627 | 0.227 | 0.125 | 0.144 |
| SDI | 0.092 | 0.355 | 0.592 | 0.24 | 0.131 | 0.171 |
| MDI | -0.003 | 0.951 | 0.643 | 0.221 | 0.122 | 0.162 |
| Submodels | 0.085 | 0.41 | 0.607 | 0.237 | 0.13 | 0.167 |
| Surrogate splits | 0.091 | 0.849 | 0.617 | 0.238 | 0.13 | 0.136 |

**Reference performance**

On the complete development data, flexible logistic regression and random forest prediction models have more or less equivalent performances in terms of calibration. [TODO: add other metrics, think about using a table, in-line values, or a figure like the one below.]



**Root mean squared error**

Root mean squared error (RMSE) tells us how well the original probability of Y could be recovered based on the incomplete predictor information in the validation set. Overall, imputation techniques for handling missing data show lower RMSEs than the non-imputation techniques (the box of submodels and surrogate splits). An exception to this is single draw imputation, which has the worst performance in terms of RMSE. The box of submodel technique (BOS) seems to work well with flexible logistic regression, but less suited for a random forest prediction model. Surrogate splits show a wide range of RMSEs across simulations. In short, the best missing data handling techniques for the flexible logistic regression prediction model are box of submodels, multiple draw imputation and conditional mean imputation; the best technique for the random forest model is multiple draw imputation.

**Brier score**

Brier score’s interpretations are similar to that of the RMSE, but than with respect to the observed binary realization of Y. Again, we see that single draw imputation is the least suited for recovering Y from the incomplete data. Multiple draw imputation has the best performance across the two prediction models, but box of submodels and conditional mean imputation work well with flexible logistic regression models as well.

**C-index**

In Figure x we refer to the c-index as AUC [TODO: change this in the figure]. The C-index is a performance measure quantifying the discriminatory ability of the different methods. Most of the methods have similar performance in terms of discrimination. Clear exception is the single draw imputation missingness technique in combination with both FLR and RF prediction models. These methods do not seem able to discriminate between cases with and without the outcome (Y=1 and Y=0, respectively).

**Calibration-in-the-large**

[TODO: re-write this] Calibration in-the-large, called ‘Intercept’ in Figure x, has an optimal value of zero. The method closest to perfect calibration in-the-large is BOS in combination with FLR. Overall, multiple draw imputation works best.

**Calibration slope**

[TODO: re-write this] Ideally, the calibration slope is equal to one. Just like the calibration in-the-large, BOS with FLR performs well, followed by multiple draw imputation with both prediction models. Now, we also observe good calibration for conditional mean imputation with FLR. Single draw imputation and BOS with RF have terrible performance in terms of the calibration slope.

# Discussion

This simulation study aimed to evaluate the effectivity of using real-time missing data handling strategies to handle missing predictor values in individual patients. We considered JMI, submodels and surrogate splits for the real-time handling of missing data when using either a flexible logistic regression or random forest model. Our simulation study showed that the optimal choice of missing data handling technique may be dependent on the preferred prediction model. The box of submodels technique seems better suited for use with a flexible logistic regression prediction model than with random forests. Overall, JMI showed the best performance (although varying with the specific choice of imputations). Our results suggest that built-in mechanisms such as surrogate splits, when compared with the other missing data handling approaches in this simulation study, show severe miscalibration for the low end and high end of predicted risks.

The performance of JMI for each of the modelling techniques depends on the method of implementation. Conditional mean imputation and multiple imputation (i.e., average over multiple draws) both performed, in terms of calibration and discrimination, much better than the single imputation variant. With a random forest as prediction model, multiple imputation performed more consistently, in terms of calibration and discrimination, than imputing the conditional mean. The difference in performance between the multiple imputation and conditional mean variant, when used for a random forest, may be explained by the congeniality, or compatibility, of the imputation model. Briefly, it means that the random forest, when compared to the flexible logistic regression, may be better at surmising the information provided to it as (non-linear) input from the completed data. When compared to conditional mean imputation, multiple imputation is ultimately less (parametrically) restrictive and allow for more variability and as such play more to the strength of a random forest.

Previous work has shown that the performance of JMI is also associated with the correlations between predictor variables, and that low correlations were associated with limited performance, in terms of calibration and discrimination (12). Since highly correlated variables are unlikely to all be used in the same prediction model it is likely that, when only predictor values are used to inform the imputation procedure, the accuracy of JMI is limited. However, the amount of information able to be leveraged from a patient can generally be much higher when other, auxiliary, variables (i.e., not part of the prediction model) are included (12). To prevent a similar limitation in this study, correlations were kept sufficiently high for JMI. The generated correlations may be limiting the propagation of the imputation methods to more realistic settings as they are slightly higher than usually observed in clinical settings. Under these circumstances the incorporation of auxiliary variables may be necessary for suitable imputation performance.

Similarly, the deficient performance of surrogate splits may be explained by the high dependency on the correlation between the missing predictor value and the surrogate replacement value (22). However, in contrast with JMI, surrogate splits depend on a sequence of singular surrogate attributes for each of the nodes with a missing predictor value, whereas JMI draws from the full conditional of the missing predictor. As a result, it may be that the correlations in this simulation study, however high, are not high enough to guarantee satisfactory surrogate splitting.

The use of submodels seems to work well for both modelling techniques and results in optimal calibration in the presence of mining predictor values. Given that a submodel approach does not in any way depend on the interrelationship between predictor variables is compelling and seems to be an advantage over the other methods evaluated in this simulation study. When used for a random forest however, the performance is much worse, in terms of calibration and discrimination. This may be explained by the fact that less predictors ultimately restrict how much a random forest may vary between each tree (23). Briefly, random forests use a combination of a random subspace method (i.e., random combinations of features) and bagging (i.e., random sample of observations). In other words, if there are less features available, as is the case in a submodel approach, the number of possible trees is limited.

[TODO: Laatste alinea met pakende uitsmijter toevoegen]

**May be added, depending on the results:**

* Gelaagd complexiteit toevoegen
* MNAR simulatie

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